

Ray-traced tropospheric slant delays for space geodetic techniques

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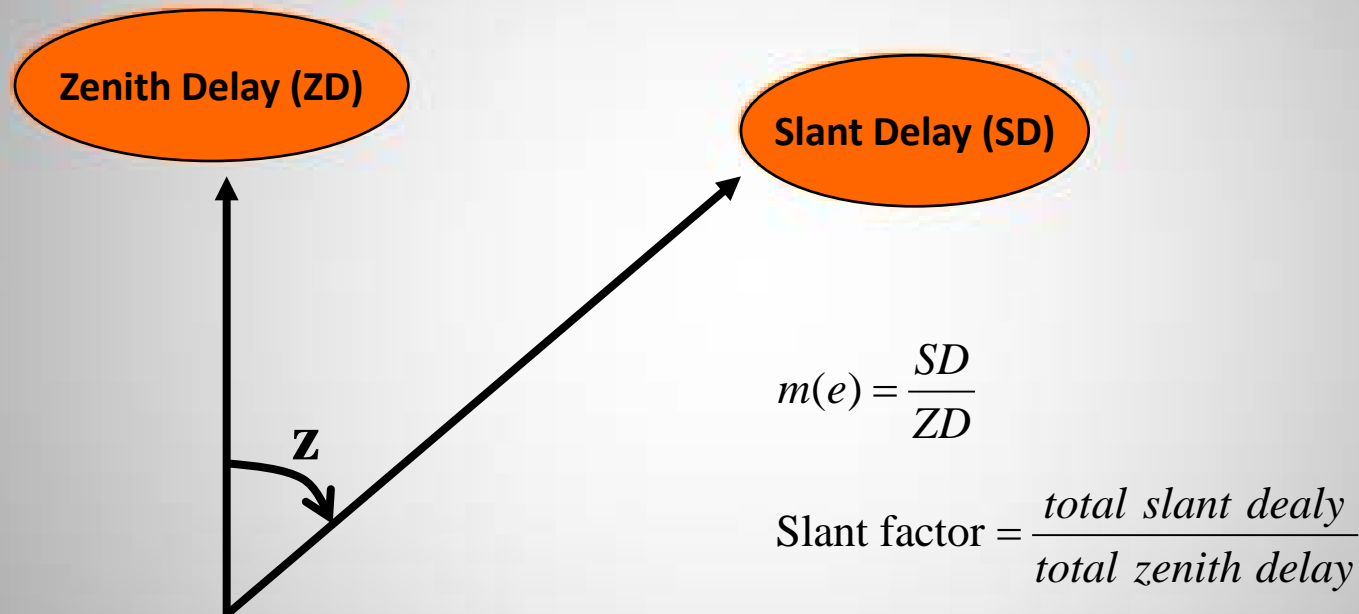
Harald Schuh

Geodätische Woche 2010

Köln, 5-7 Oktober 2010

- Troposphere delay as an error source for all space geodetic techniques
- Model of total delay as a function of surface meteorological parameters only
- Most commonly used model is that of Saastamoinen (1972)
- Parameter estimation techniques (using the least squares method)
- Mapping function to calculate delays for each observation

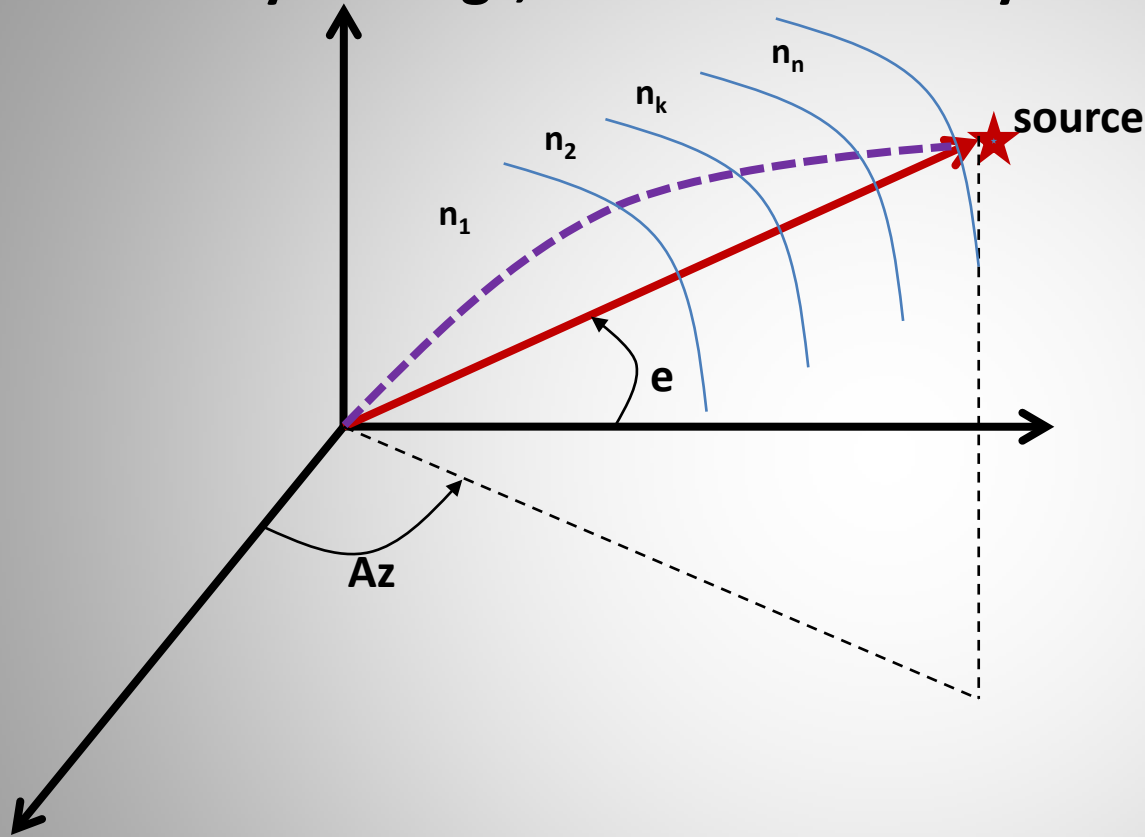
- Concept of mapping function



Zenith delay can be determined as a function of:

- Meteorological data at the site
- Coordinates (height and latitude of the site)

- “Direct ray-tracing”, to find slant delay directly, along the **true path**



- Solution: **Suitable mathematical model** + **Atmospheric data set**

↓
2D or 3D

↓
Numerical Weather models (NWM)

1. Mathematical model for 3D and 2D Ray-tracing systems

(1)

- **Eikonal equation**

$$[\nabla L(\vec{r})]^2 = n(\vec{r})^2$$

L : optical path length,

\vec{r} : vector of positions,

n : refractive index,

∇ : gradient operator w.r.t positions

.Refractivity, as a function of meteorological parameters

$$N = k_1 \frac{p_d}{T} + k_2 \frac{e}{T} + k_3 \frac{e}{T^2} \longrightarrow n = 1 + N \times 10^{-6}$$

1. Mathematical model for 3D and 2D Ray-tracing systems

(2)

- **Partial derivatives of the refractivity in spherical coordinate system**

-16 points around a specific point (point of ray-path), for computing partial derivatives $\frac{\partial n}{\partial \lambda}$, $\frac{\partial n}{\partial \theta}$ and $\frac{\partial n}{\partial r}$

- Spline interpolation for value of refractivity (or refractive index) in each point

- **Special case : 2D Ray-tracer (ignoring out-of-plane components)**

$$\frac{\partial n}{\partial \theta} = 0 \quad \frac{\partial n}{\partial \lambda} = 0$$

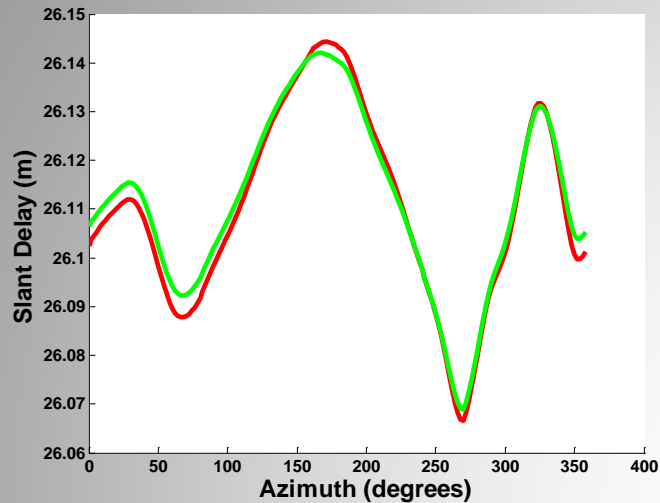
2. Practical considerations for developing a ray-tracing method at TU Wien

- **Linear interpolation for temperature and exponential for pressure and water vapor pressure**
- **A pre-calculation process for compiling and converting ECMWF file to refractivity (N) profiles for each grid point**
- **Rüeger “best average” constants for refractivity (Rüeger,2002)**
- **US standard atmosphere of 1976 for meteorological data above upper limit of ECMWF up to 76 Km.**
- **Horizontal interpolation (spline, bilinear, weighted mean,...)**

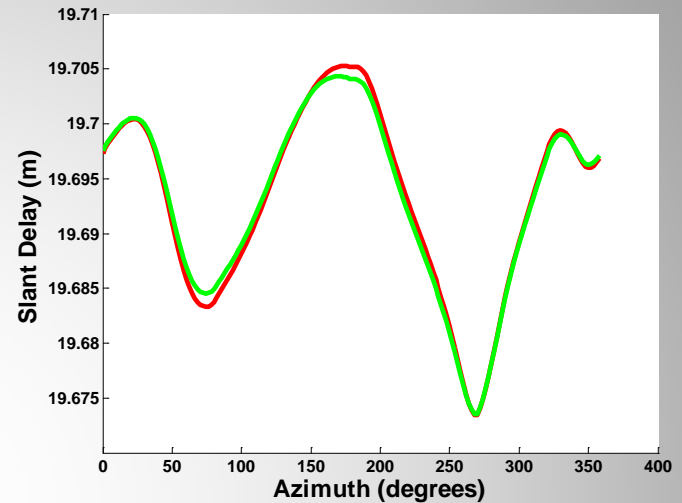
3. Results for VIE ray-tracers

(1)

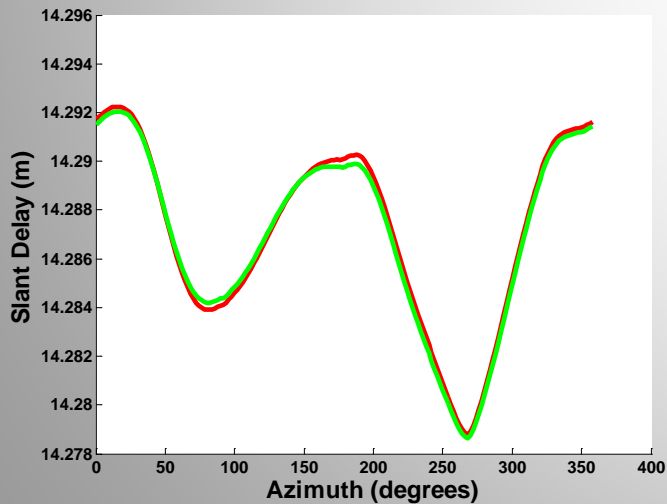
Computed delays for TSUKUBA site, using 2D and 3D ray-tracers



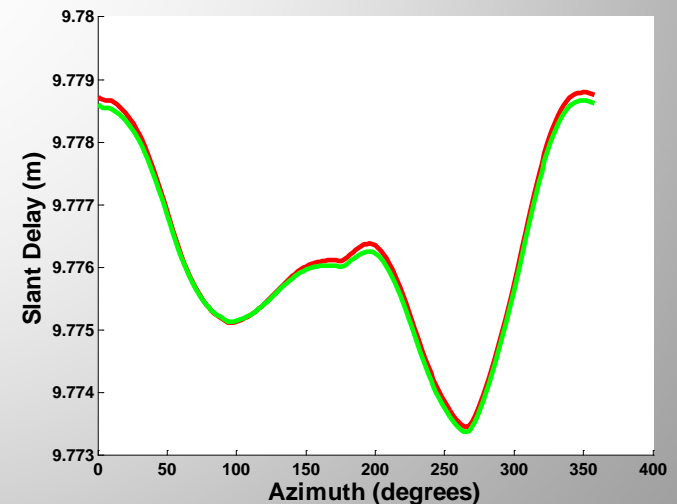
5-deg. Elevation angle



7-deg. Elevation angle



10-deg. Elevation angle



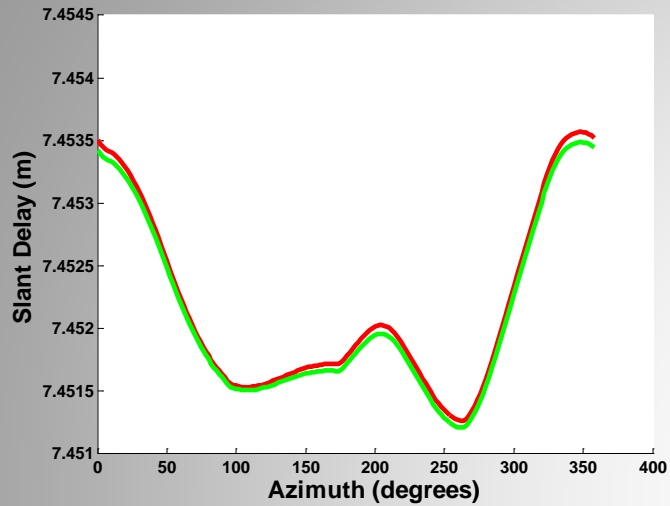
15-deg. Elevation angle

red: 2D, green: 3D

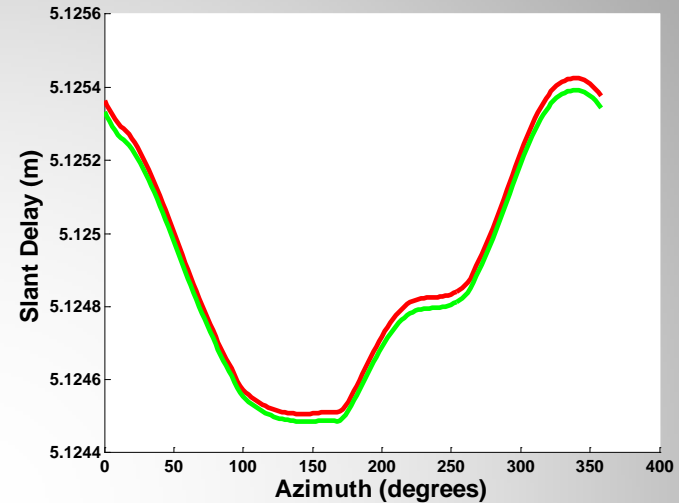
3. Results for VIE ray-tracers

(2)

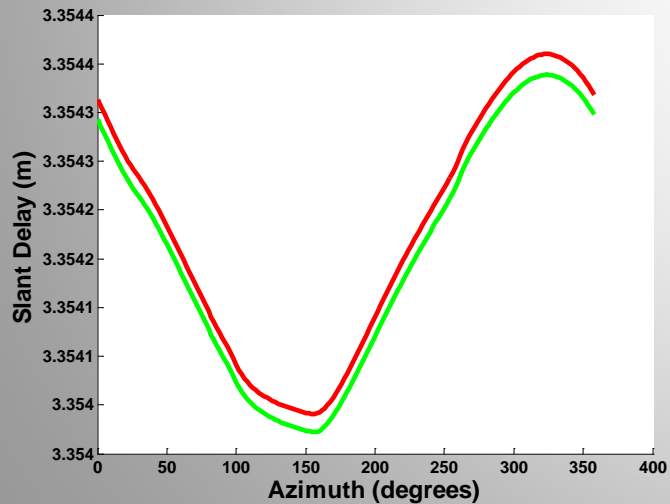
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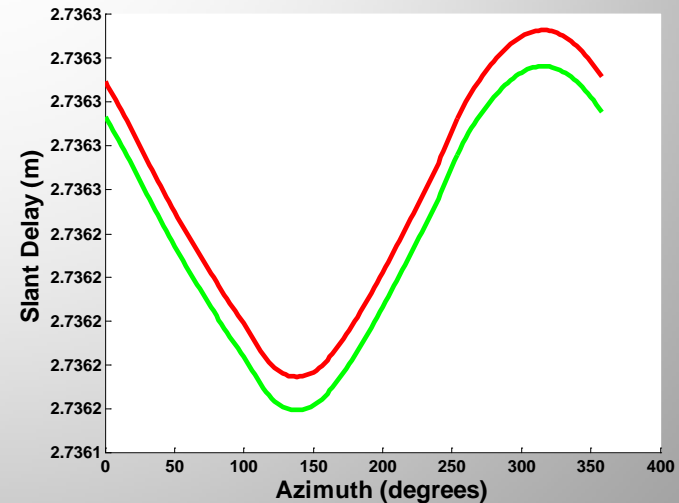
20-deg. Elevation angle



30-deg. Elevation angle



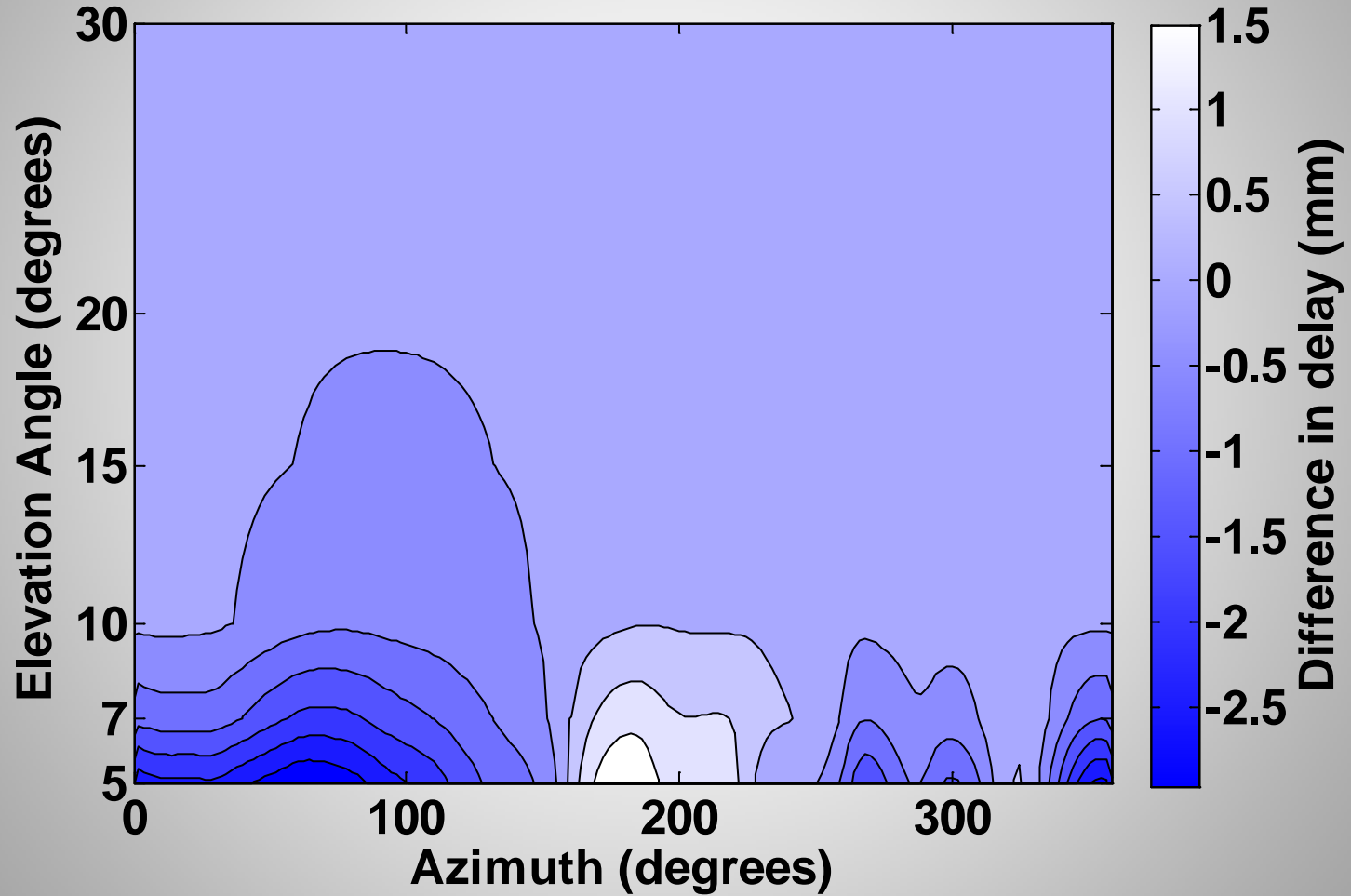
50-deg. Elevation angle



70-deg. Elevation angle

red: 2D, green: 3D

Differences in total delay
VIE-2D vs VIE-3D
TSUKUBA 12.08.2008



4. Results of ray-tracing campaign

(1)

- ❖ **Aim: investigations about effect of different elements of ray-tracers on the final results and preparing benchmarking results for other ray-tracers**
- ❖ **Task: Computing total ray-traced delays at every degree (outgoing) elevation ($>5^\circ$) and azimuth, plus the bending effect at the first epoch (0 UT)**
- ❖ **Under the umbrella of IAG WG 4.3.3 chaired by Thomas Hobiger**
- ❖ **First half of 2010**

Participants in this benchmarking campaign

- 1) UNB Raytracer : Felipe Nievinski, Landon Urquhart and Marcelo Santos (University of New Brunswick, Canada)
- 2) KARAT Raytracer (2D and 3D): Thomas Hobiger et al. (NICT, Japan)
- 3) Horizon-Eikonal : Pascal Gegout (GRGS, Toulouse, France)
- 4) GFZ: Florian Zus et al. (GFZ, Potsdam, Germany)
- 5) Vienna Raytracer (2D and 3D) : Vahab Nafisi , Dudy Wijaya, Johannes Böhm (Vienna University of Technology, Austria)

4. Results of ray-tracing campaign

(3)

Different considerations, in different ray-traces

Ray-tracer	NWM	Upper limit of Trop. (km)	Supplementary atmosphere	Radius of curvature of the Earth	Interpolation methods
GFZ	ECMWF-model level	150	-	local radius of curvature of the reference ellipsoid	Refractivity: log-linear interpolation
Horizon-eikonal	ECMWF-model level	80	-	WGS84 reference ellipsoid	Refractivity: exponential
KARAT- Thayer	ECMWF-pressure level	86	US 76	Euler's formula	Temperature and relative humidity :linear Pressure.: logarithmically
KARAT-Eikonal	ECMWF-pressure level	86	US 76	Euler's formula	Temperature and relative humidity :linear Pressure.: logarithmically
UNB- bent3D	ECMWF-pressure level	100	CIRA86	ellipsoidal coordinates	Temperature and specific humidity: linear, Pressure: logarithmically
VIE-3D	ECMWF-pressure level	76	US 76	Gaussian mean curvature	Temperature: linear Pressure and water vapor pressure: exponential
VIE-2D	ECMWF-pressure level	76	US 76	Gaussian mean curvature	Temperature: linear Pressure and water vapor pressure: exponential

Data set # 1

TSUKUBA site (Japan)

$$\phi = 36^{\circ}.1031$$

$$\lambda = 140^{\circ}.0887$$

$$h = 85.09m$$

$$N = 38.92m$$

Epoch : **12.08.2008**, 0^h

ECMWF Model, 0.1×0.1

Data set # 2

WETTZELL site (Germany)

$$\phi = 49^{\circ}.15$$

$$\lambda = 12^{\circ}.88$$

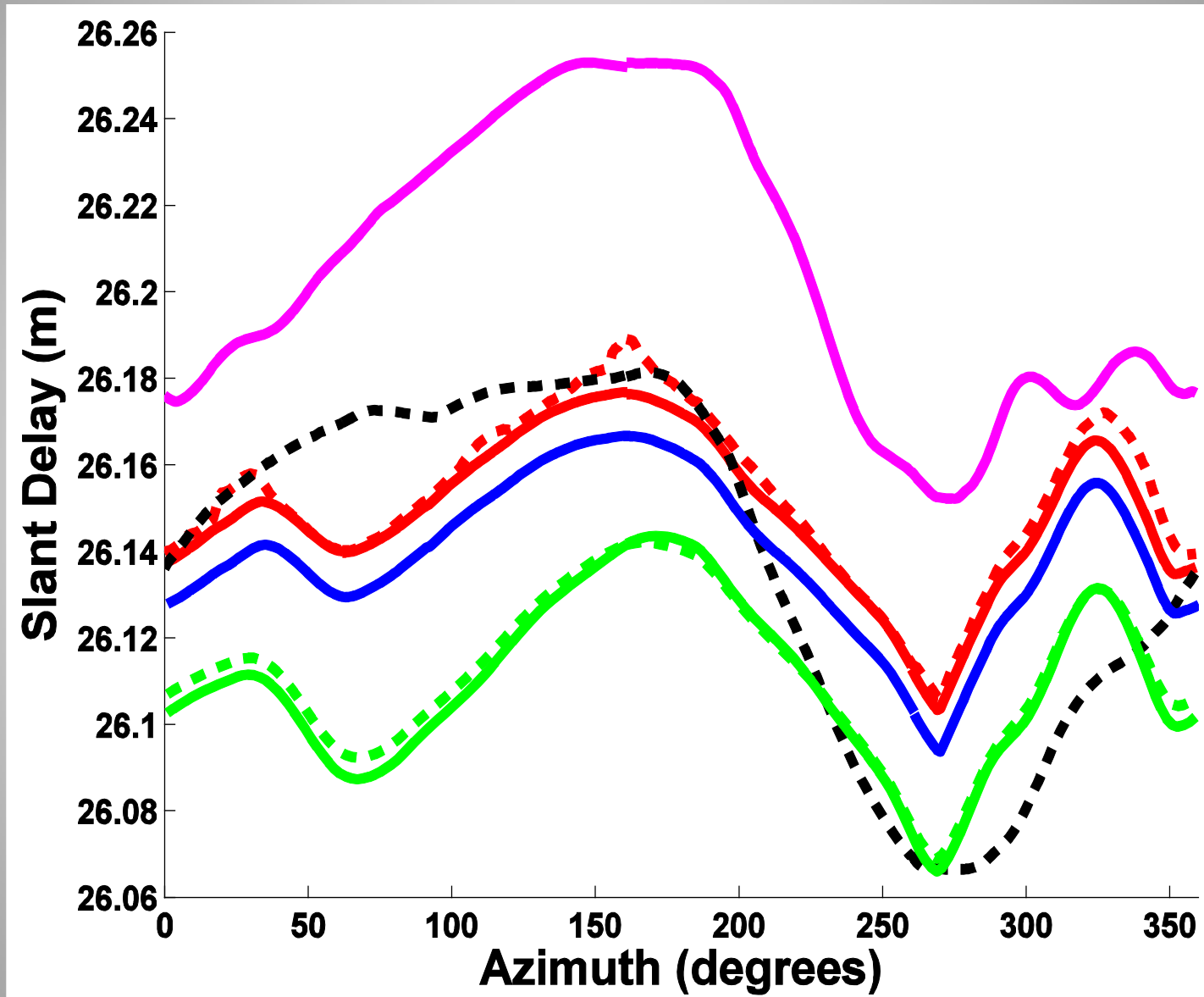
$$h = 699.56m$$

$$N = 50m$$

Epoch : **01.01.2008**, 0^h

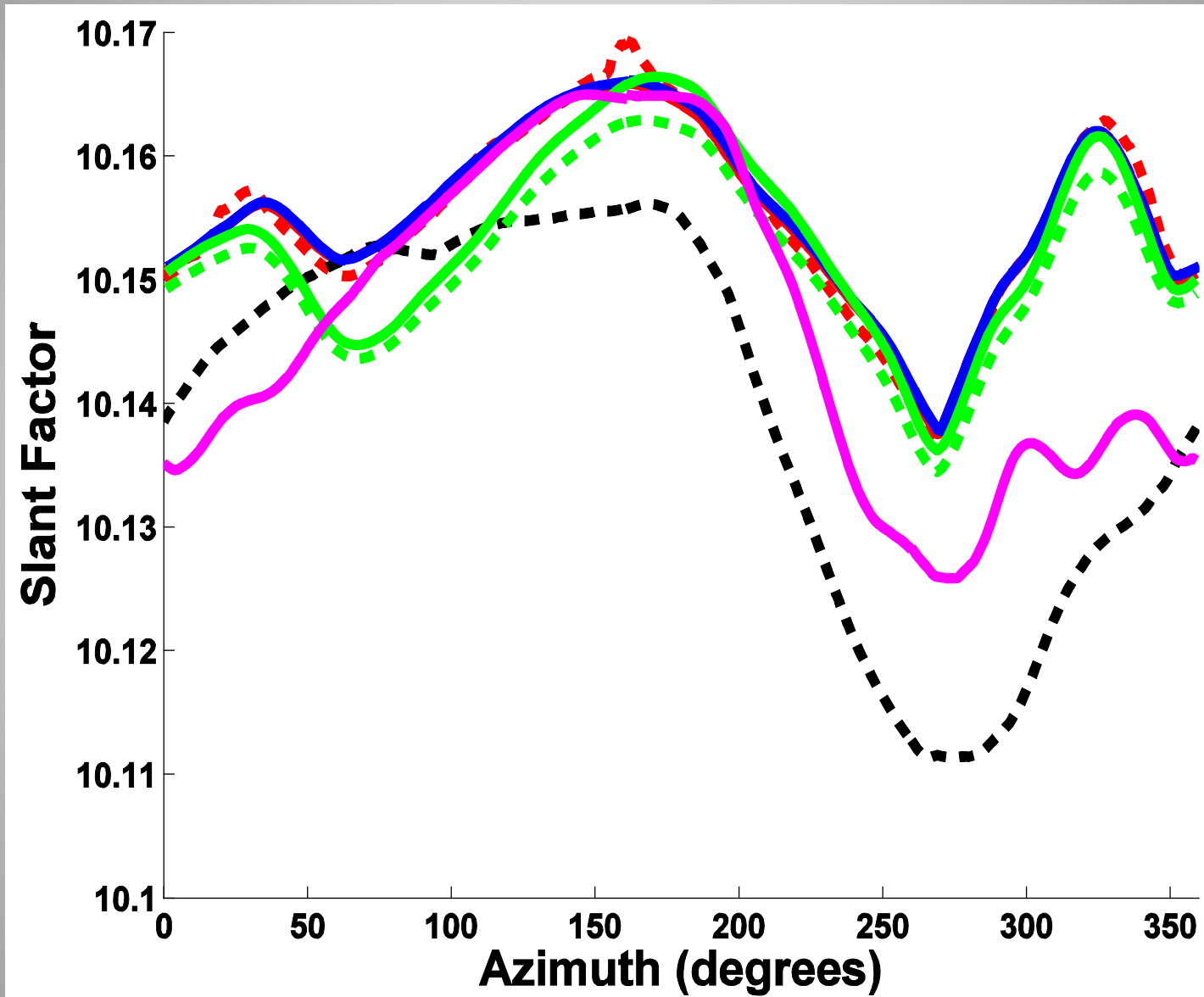
ECMWF Model, 0.1×0.1

4. Results of ray-tracing campaign – Tsukuba, 5 deg. Elevation angle (5)



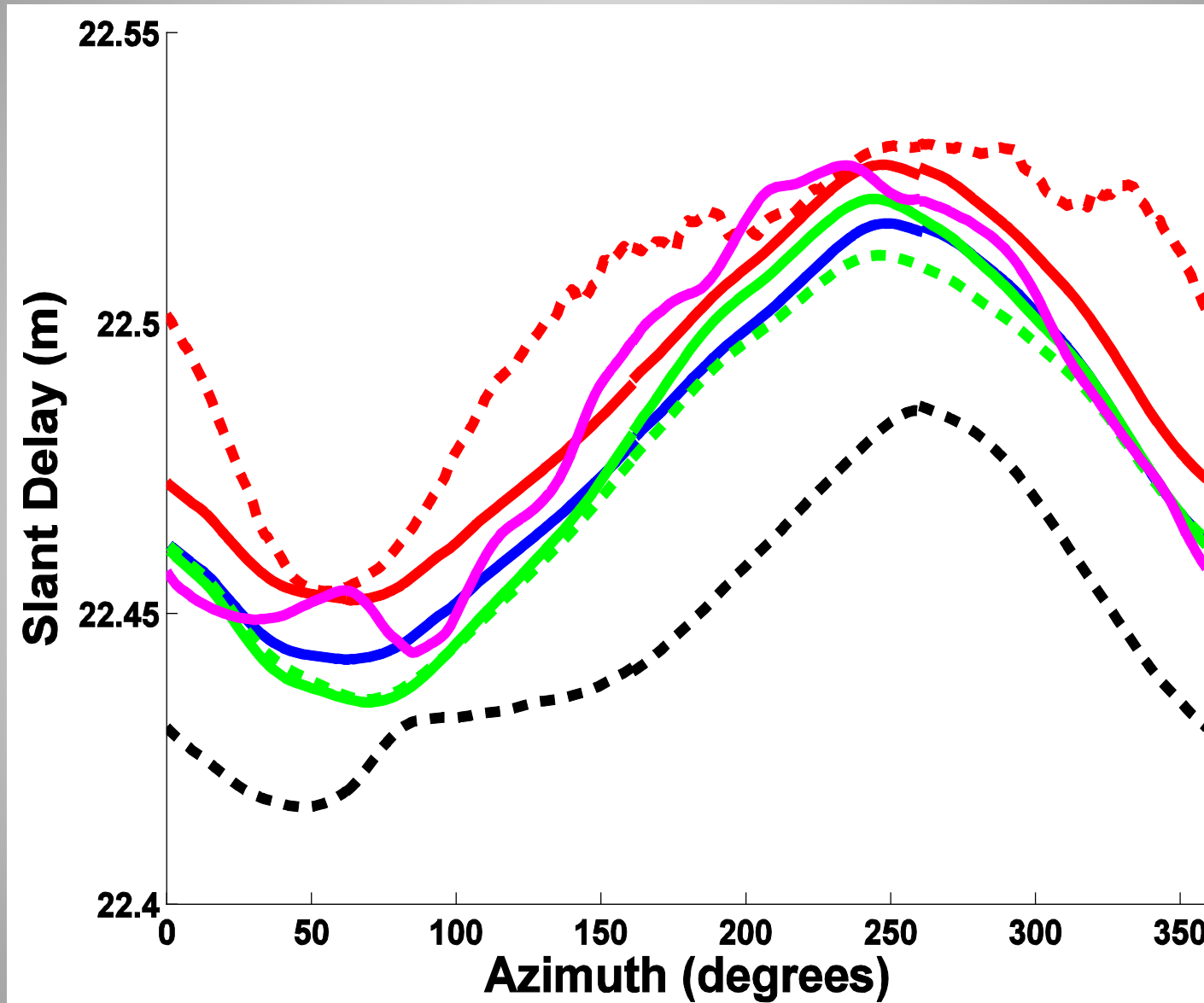
12.08.2010

4. Results of ray-tracing campaign – Tsukuba, 5 deg. Elevation angle (6)



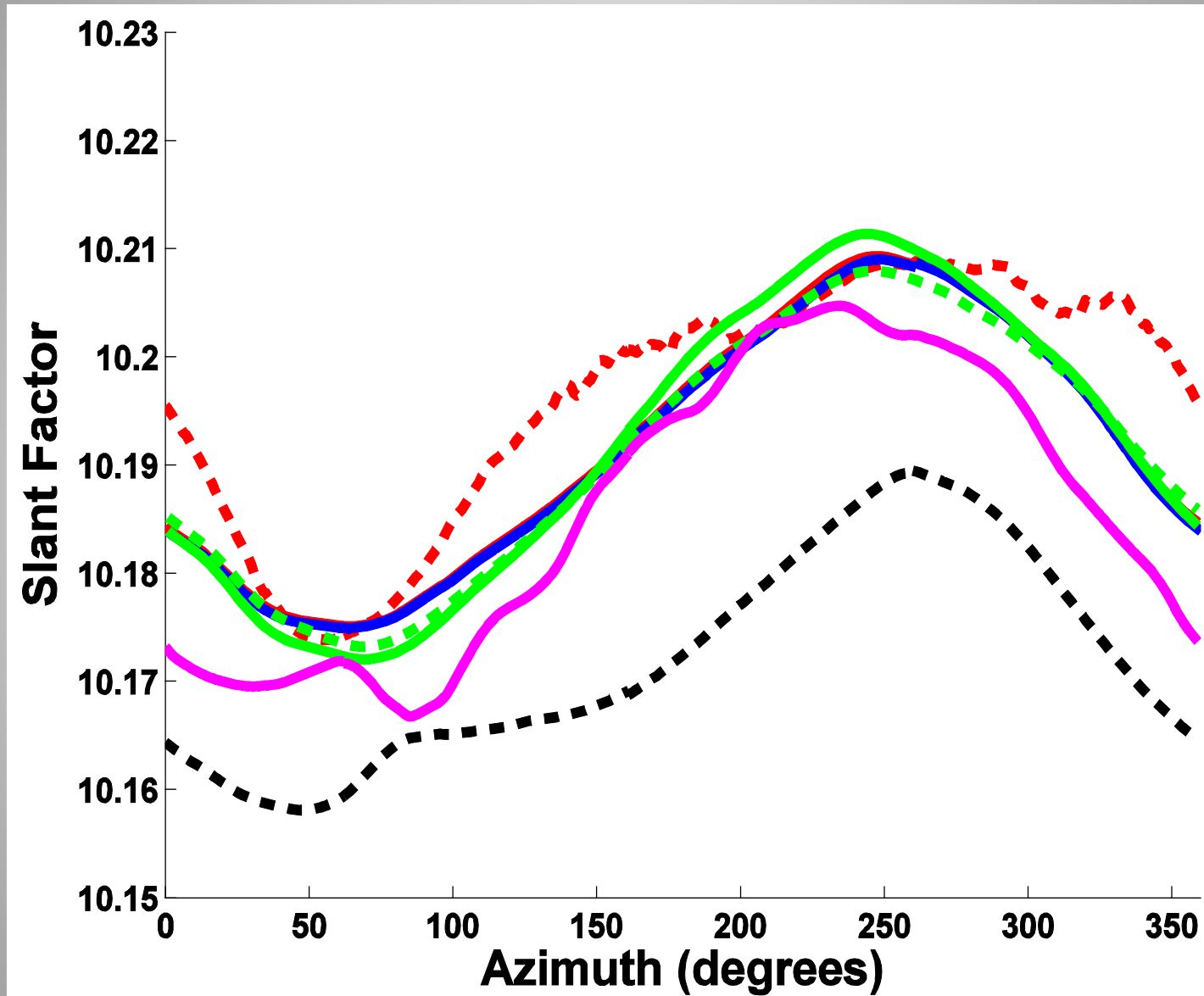
12.08.2010

4. Results of ray-tracing campaign – Wetzell, 5 deg. Elevation angle (7)



01.01.2008

4. Results of ray-tracing campaign – Wetzell, 5 deg. Elevation angle (8)



01.01.2008

Rule of thumb: The error in the station height is approximately $1/5$ of the slant delay error at the 5 degrees elevation angle (Böhm, 2004)



For precision of 2mm for station heights we must care about elements of ray-tracer system

For a precision of 2 mm in station height, the biases between slant factors have to be smaller than 0.005. If the zenith delay is 2 m this corresponds to 1 cm at 5 degrees elevation, and $1/5$ th of this is 2 mm.

We need to estimate residual zenith delay

- **Developing a 3D ray-tracer based on Eikonal equation**
- **Some simplifications for a 2D ray-tracer (ignoring out-of-plane components)**
- **Discrepancies between results of different ray-tracers (ray-tracing campaign), because of different interpolation and extrapolation methods, upper limit of troposphere, data sets**

- Focus on different Numerical Weather Models in future
- Validation of results obtained by VIE ray-tracers, using VLBI observations
- Ray-traced delays as a part of Vienna VLBI Software (VieVS) in future

